

ELECTRONIC DEVICES & CIRCUITS

Module 6

DACs

S3 CSE KTU

prepared by

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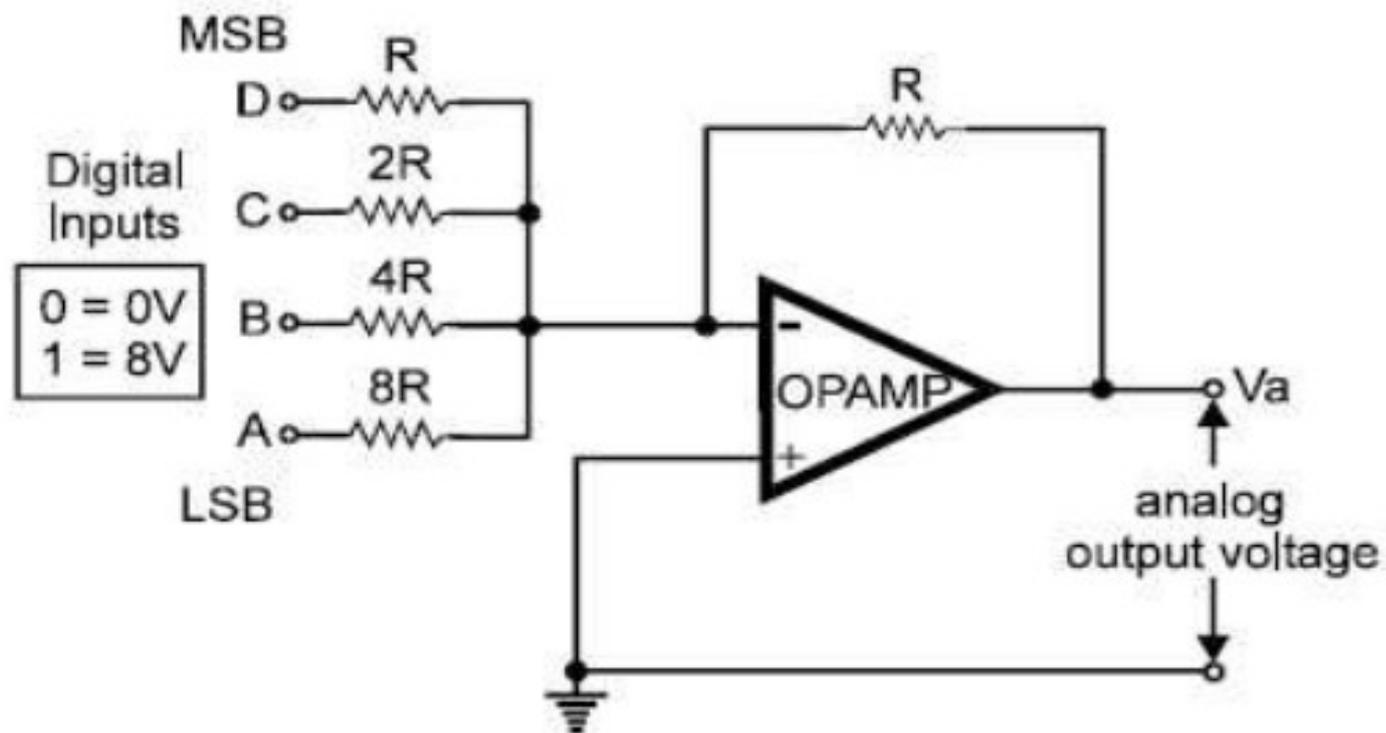
DIGITAL TO ANALOG CONVERTER

- **A DAC (Digital-to-Analog Converter) is used to convert a digital signal to the analog format.**
- **For example, music stored in a DVD in digital format must be converted to an analog voltage for playing out on a speaker.**
- **Real signals (e.g., a voltage measured with a thermocouple or a speech signal recorded with a microphone) are analog quantities, varying continuously with time.**
- **An ADC (Analog-to-Digital Converter) is used to convert an analog signal to the digital format.**
- **Digital format offers several advantages: digital signal processing, storage, use of computers, robust transmission, etc.**

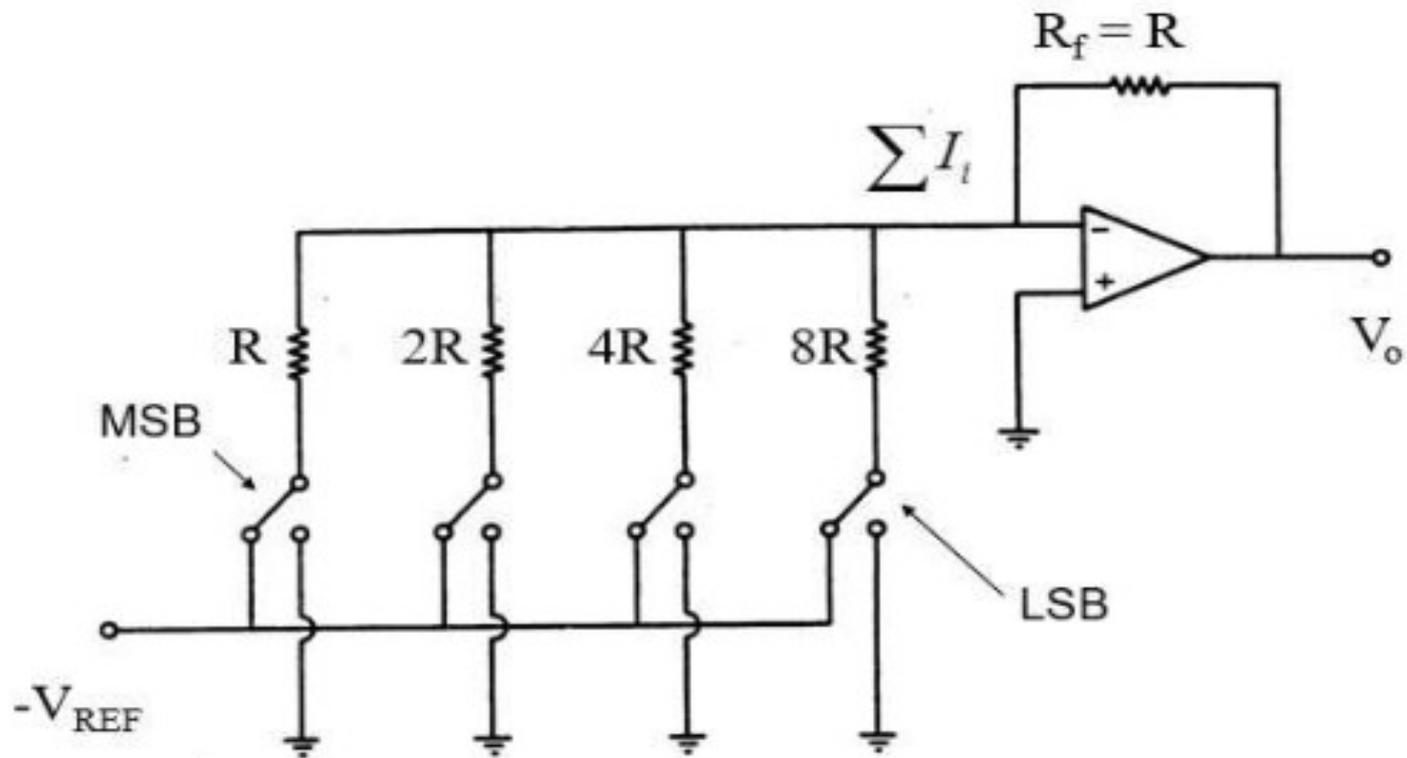
DAC - INTRODUCTION

- **The process of converting digital signal into equivalent analog signal is called D/A conversion.**
- **The electronics circuit, which does this process, is called D/A converter.**
- **The circuit has 'n' number of digital data inputs with only one output.**
- **Basically, there are two types of D/A converter circuits:**
 - 1. Weighted resistors D/A converter circuit and**
 - 2. Binary ladder or R-2R ladder D/A converter circuit.**

WEIGHTED RESISTORS D/A CONVERTER



BINARY WEIGHTED RESISTOR



- **Here an opamp is used as summing amplifier.**
- **There are four resistors R , $2R$, $4R$ and $8R$ at the input terminals of the opamp with R as feedback resistor.**
- **The network of resistors at the input terminal of opamp is called as variable resistor network.**
- **The four inputs of the circuit are D, C, B & A.**
- **Input D is at MSB and A is at LSB.**
- **Here we shall connect 8V DC voltage (say) as logic-1 level.**
- **So we shall assume that $0 = 0V$ and $1 = 8V$.**
- **Now the working of the circuit is as follows.**
- **Since the circuit is summing amplifier, its output is given by the following equation –**

$$V_o = -R \left(\frac{D}{R} + \frac{C}{2R} + \frac{B}{4R} + \frac{A}{8R} \right)$$

- **When digital input of the circuit DCBA = 0011, then putting these value in previous equation, we get**

$$V_o = -R \left(\frac{0}{R} + \frac{0}{2R} + \frac{8V}{4R} + \frac{8V}{8R} \right) = -R \left(\frac{8V}{4R} + \frac{8V}{8R} \right) = -3V$$

- **In this way, when digital input changes from 0000 to 1111, output voltage (Vo) changes proportionally.**
- **This is given in the conversion chart.**

| Digital inputs | | | | Analog output |
|----------------|---|---|---|---------------------------|
| D | C | B | A | Voltage (V _a) |
| 0 | 0 | 0 | 0 | 0V |
| 0 | 0 | 0 | 1 | -1V |
| 0 | 0 | 1 | 0 | -2V |
| 0 | 0 | 1 | 1 | -3V |
| 0 | 1 | 0 | 0 | -4V |
| 0 | 1 | 0 | 1 | -5V |
| 0 | 1 | 1 | 0 | -6V |
| 0 | 1 | 1 | 1 | -7V |
| 1 | 0 | 0 | 0 | -8V |
| 1 | 0 | 0 | 1 | -9V |
| 1 | 0 | 1 | 0 | -10V |
| 1 | 0 | 1 | 1 | -11V |
| 1 | 1 | 0 | 0 | -12V |
| 1 | 1 | 0 | 1 | -13V |
| 1 | 1 | 1 | 0 | -14V |
| 1 | 1 | 1 | 1 | -15V |

BINARY WEIGHTED RESISTOR

Result:

$$\sum I = V_{REF} \left(\frac{B_3}{R} + \frac{B_2}{2R} + \frac{B_1}{4R} + \frac{B_0}{8R} \right)$$

$$V_{OUT} = I \cdot R_f = V_{REF} \left(B_3 + \frac{B_2}{2} + \frac{B_1}{4} + \frac{B_0}{8} \right)$$

Vref is -ve for getting +ve voltage

□ B_i = Value of Bit i

For 3 bit DAC $V_{OUT} = V_{REF} \left(B_2 + \frac{B_1}{2} + \frac{B_0}{4} \right)$

A 5-bit D/A converter produces $V_{\text{OUT}} = 0.2 \text{ V}$ for a digital input of 0001. Find the value of V_{out} for an input of 11111.

Solution

Obviously, 0.2 V is the weight of the LSB. Thus, the weights of the other bits must be 0.4 V , 0.8 V , 1.6 V , and 3.2 V respectively. For a digital input of 11111, then, the value of V_{OUT} will be $3.2 \text{ V} + 1.6 \text{ V} + 0.8 \text{ V} + 0.4 \text{ V} + 0.2 \text{ V} = 6.2 \text{ V}$.

Resolution

Resolution of a D/A converter is defined as the smallest change that can occur in the analog output as a result of a change in the digital input.

Resolution is the change in analog o/p voltage/current corresponding to change in LSB

Eg: For $V_{ref} = 5V$, o/p corresponding to LSB of a 4 bit DAC = $V_{ref}/8 = 5V/8 = 0.625V$

Resolution = $0.625V$

For $V_{ref} = 10V$, o/p corresponding to LSB = $10V/8 = 1.25V$

Resolution = $1.25V$

5 bit DAC, $V_{ref} = 10V$, change in o/p corresponding to LSB = $10V/16 = 0.625V$

$$\% \text{ resolution} = \frac{1}{\text{total number of steps}} \times 100\%$$

For an N-bit binary input code the total number of steps is $2^N - 1$.

$$\% \text{ resolution} = \frac{1}{2^N - 1} \times 100\%$$

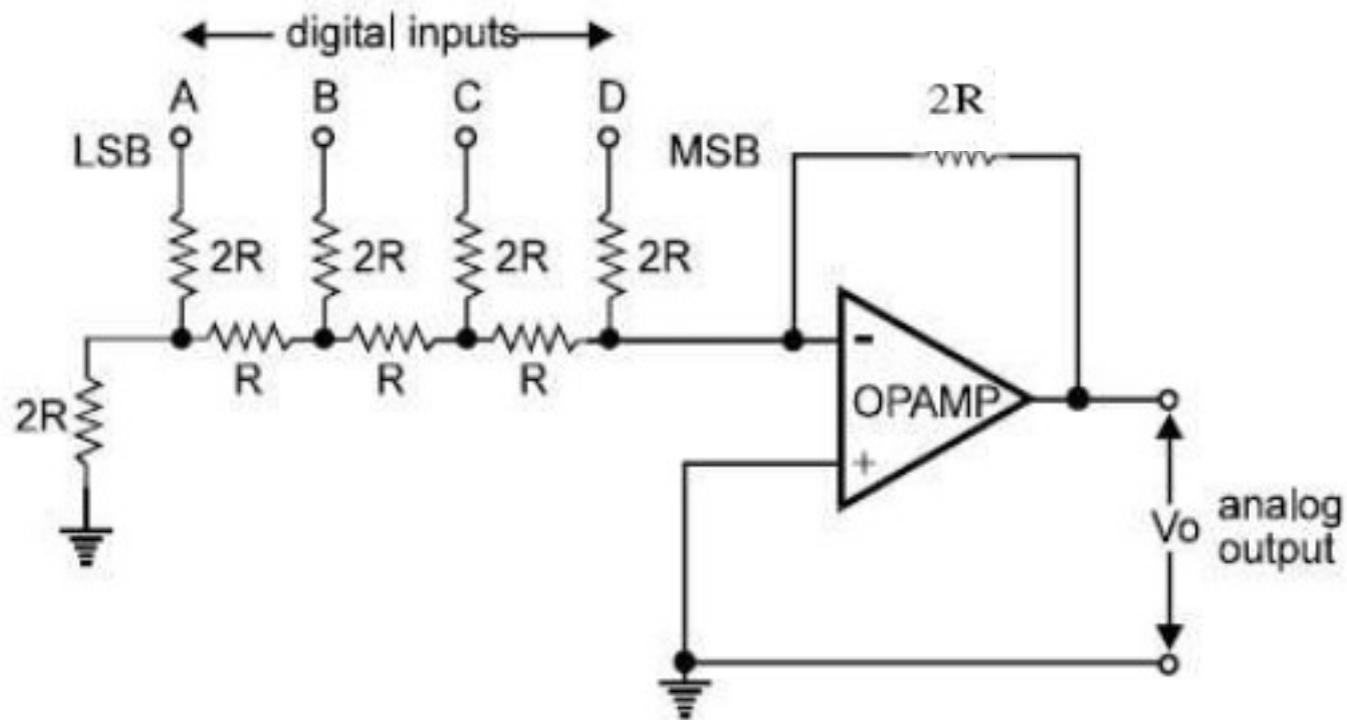
For a 10 bit DAC

$$\% \text{ resolution} = \frac{1}{2^{10} - 1} \times 100\%$$

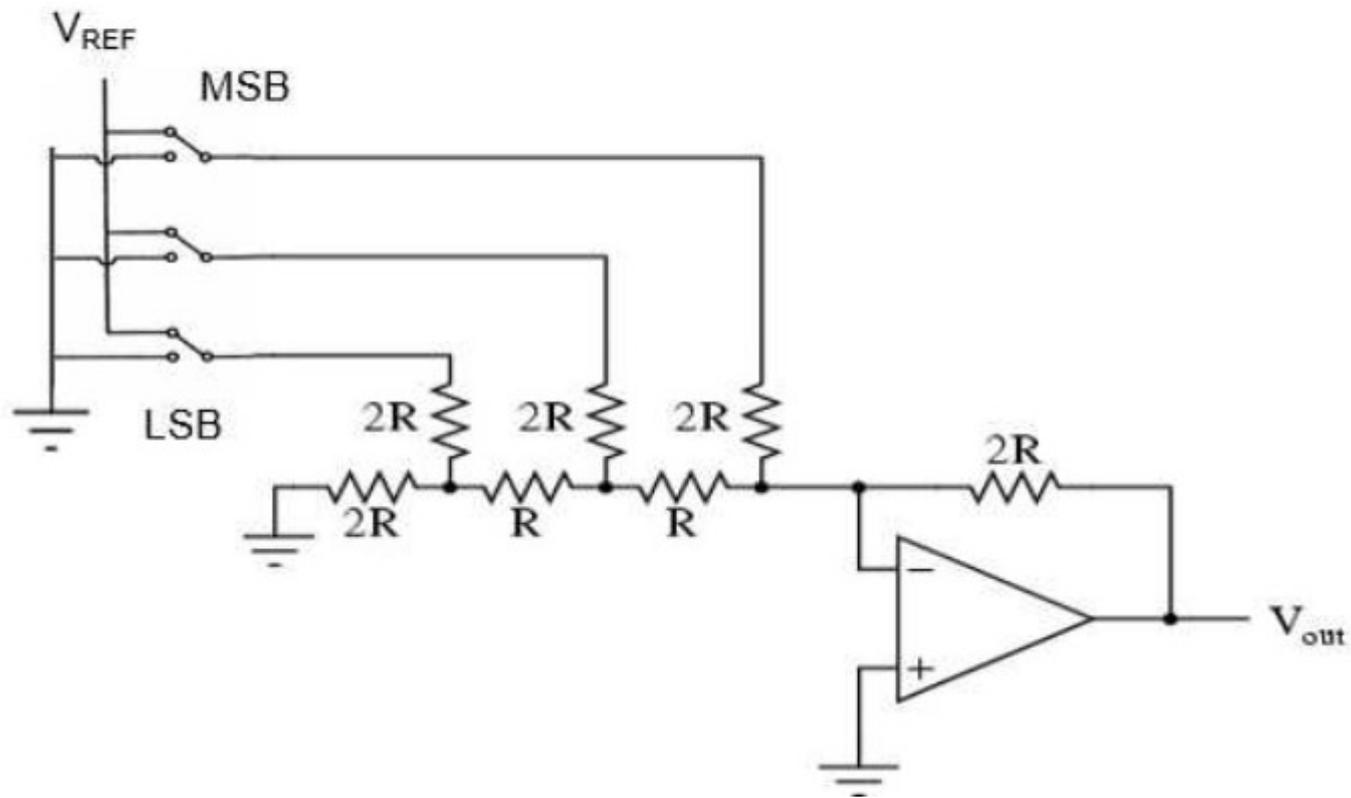
$$= \frac{1}{1023} \times 100\%$$

$$\approx 0.1\%$$

R-2R LADDER

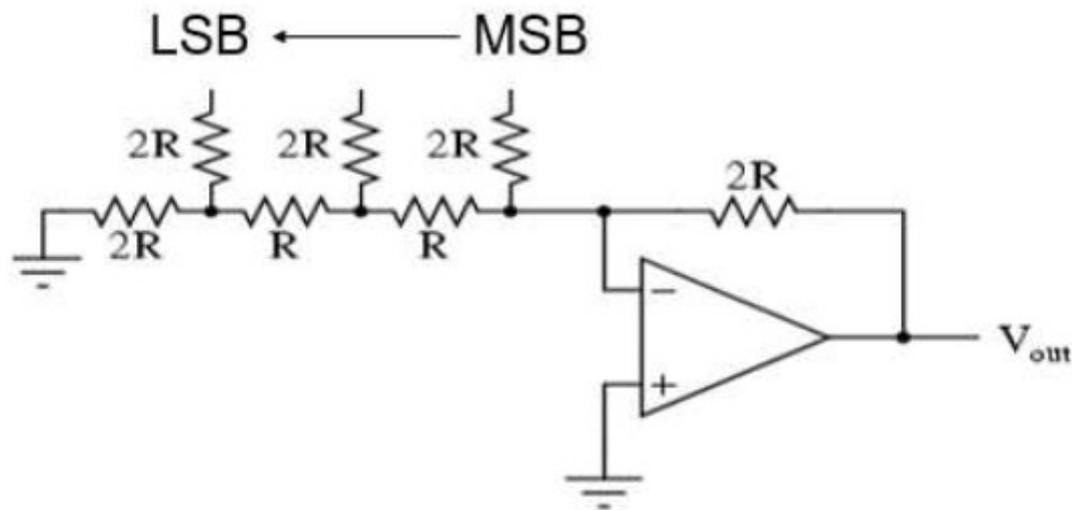


R-2R LADDER



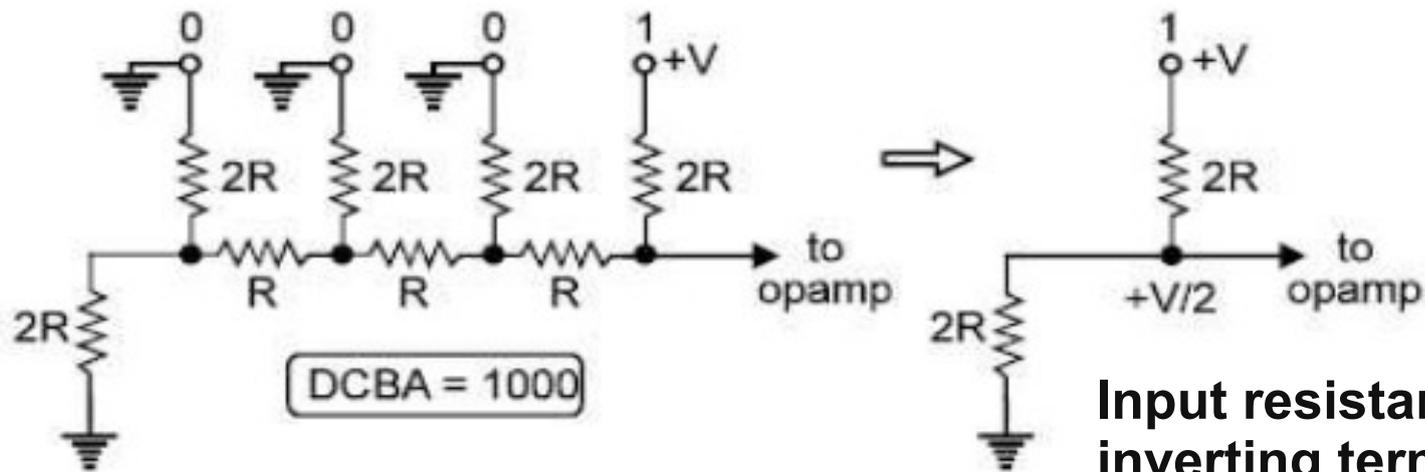
R-2R LADDER

- The less significant the bit, the more resistors the signal must pass through, before reaching the op-amp
- The current is divided by a factor of 2 at each node



- **It has only two values of resistors the R and 2R.**
- **These values repeat throughout in the circuit.**
- **The opamp is used at output for scaling the output voltage.**

- **For simplicity, we ignore the opamp in the above circuit (**
- **Now consider the circuit, without opamp.**
- **Suppose the digital input is DCBA = 1000.**



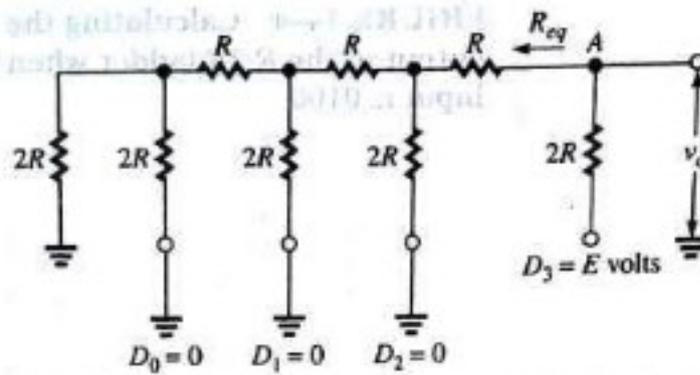
Input resistance on inverting terminal is reduced to $2R \parallel 2R = R$

- Its output is given by –

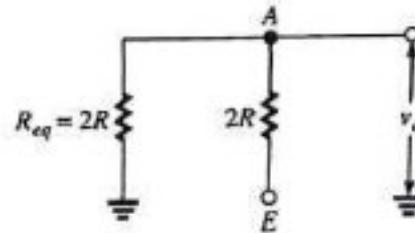
$$\text{output} = \left(\frac{2R}{2R + 2R} \right) \times (+V) = \frac{V}{2}$$

- Now suppose digital input of the same circuit is changed to **DCBA = 0100**.
- Then the output voltage will be $V/4$, when **DCBA = 0010**, output voltage will be $V/8$, for **DCBA = 0001**, output voltage will be $V/16$ and so on.

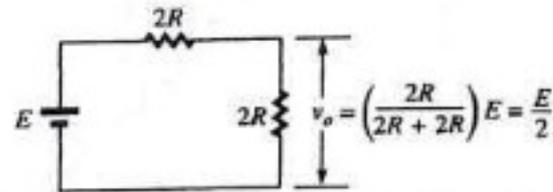
Analysis When MSB = 1



(a) When the input is 1000, $D_0, D_1,$ and D_2 are grounded (0 V) and D_3 is E volts.

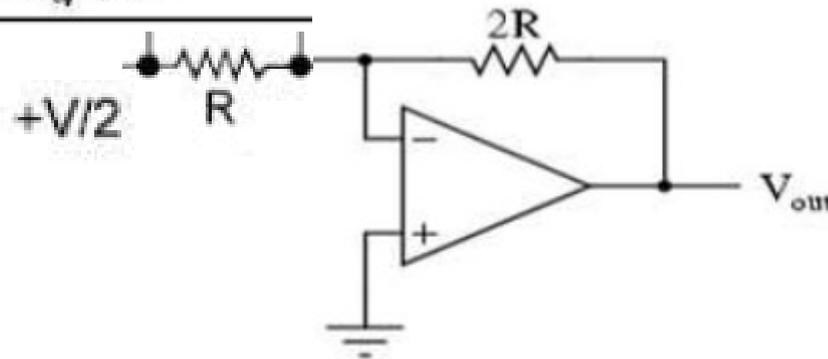


(b) The circuit equivalent to (a) when the network to the left of node A is replaced by its equivalent resistance, R_{eq} .

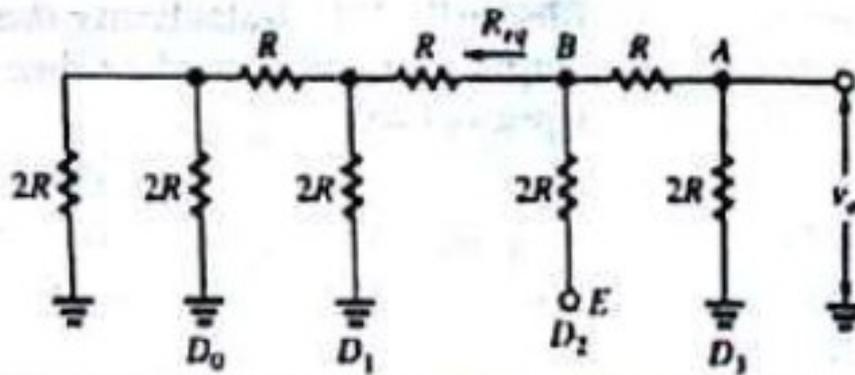


(c) Calculation of v_o using the voltage-divider rule. (Note that v_o in (b) is the voltage across $R_{eq} = 2R$.)

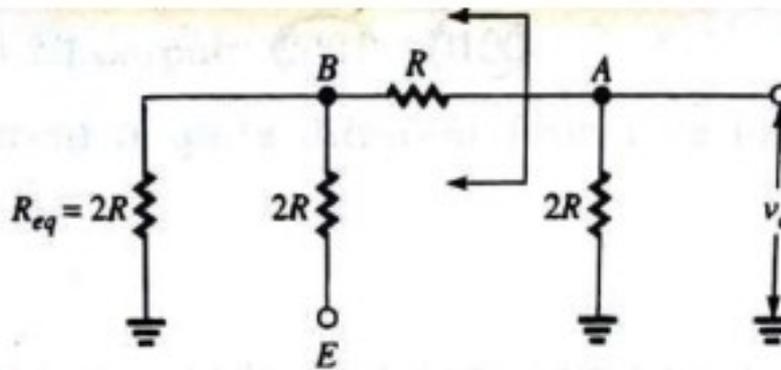
When MSB = 1,
the R-2R ladder
DAC will reduce
to



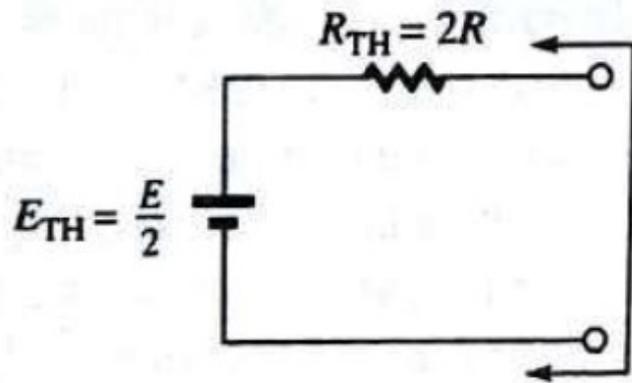
Analysis When the next highest bit = 1



(a) When the input is 0100, D_0 , D_1 , and D_3 are grounded and D_2 is E volts.



(b) The circuit equivalent to (a) when the network to the left of node B is replaced by its equivalent resistance ($2R$). The Thevenin equivalent circuit to the left of the bracketed arrows is shown in (c).

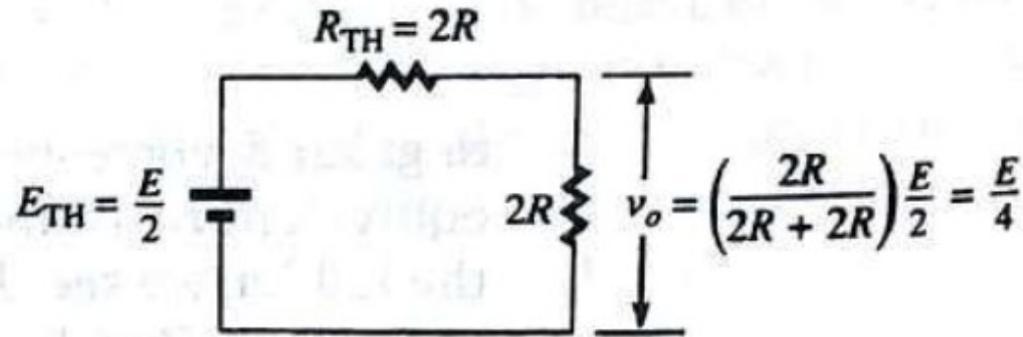


$$R_{TH} = R + 2R \parallel 2R = 2R$$

$$E_{TH} = \left(\frac{2R}{2R + 2R} \right) E = \frac{E}{2}$$

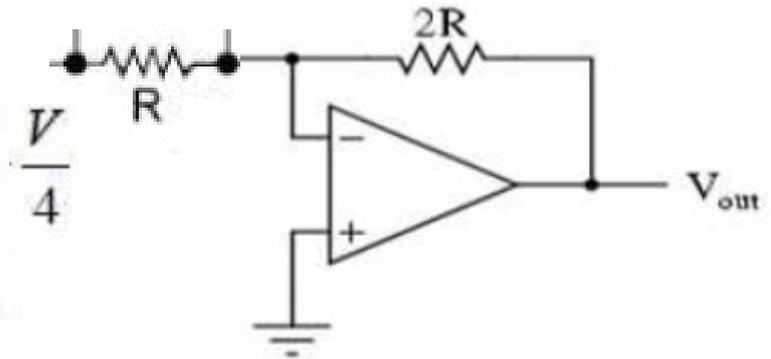
When DCBA = 0100, the R-2R ladder DAC will reduce to

(c) The Thevenin equivalent circuit to the left of node A.



$$v_o = \left(\frac{2R}{2R + 2R} \right) \frac{E}{2} = \frac{E}{4}$$

(d) Calculation of v_o using the voltage-divider rule.



- The general formula for the above circuit of R–2R ladder, including the opamp also, will be –

$$V_o = -2R/R(V_{ref} D/2 + V_{ref} C/4 + V_{ref} B/8 + V_{ref} A/16)$$

$$V_{OUT} = V_{REF} \left(B_3 + \frac{B_2}{2} + \frac{B_1}{4} + \frac{B_0}{8} \right)$$

Same as weighted resistor if gain of op-amp summing amplifier is 2

Imp: Gain of OP-AMP in weighted resistor DAC = 1

For 3 bit DAC

$$V_{OUT} = V_{REF} \left(B_2 + \frac{B_1}{2} + \frac{B_0}{4} \right)$$

PROS & CONS

| | Binary Weighted | R-2R |
|------|---|--|
| Pros | Easily understood | Only 2 resistor values Easier implementation Faster response time Easily scalable to any desired number of bits |
| Cons | Limited to ~ 8 bits Large # of resistors Susceptible to noise Expensive Greater Error | More confusing analysis |

(ii) A 4-bit Weighted resistor DAC having $R = 10 \text{ k}\Omega$ and $V_R = 10 \text{ V}$. Find its resolution and output voltage for an input 1101. (4)

$$V_{OUT} = -V_{REF} \left(B_3 + \frac{B_2}{2} + \frac{B_1}{4} + \frac{B_0}{8} \right)$$

**Resolution of 4 bit weighted resistor DAC
with $V_{ref} = 10\text{V}$ is $10/8 = 1.25\text{V}$**

(ii) A 4-bit R-2R ladder type DAC having $R = 10 \text{ k}\Omega$ and $V_R = 10 \text{ V}$. Find its resolution and output voltage for an input 1101. (4)

$$V_{OUT} = -V_{REF} \left(B_3 + \frac{B_2}{2} + \frac{B_1}{4} + \frac{B_0}{8} \right)$$

**Resolution of 4 bit R-2R ladder DAC
with $V_{ref} = 10\text{V}$ is $10/8 = 1.25\text{V}$**

% Resolution of 4 bit DAC

$$(1/15) * 100 = 6.67\%$$

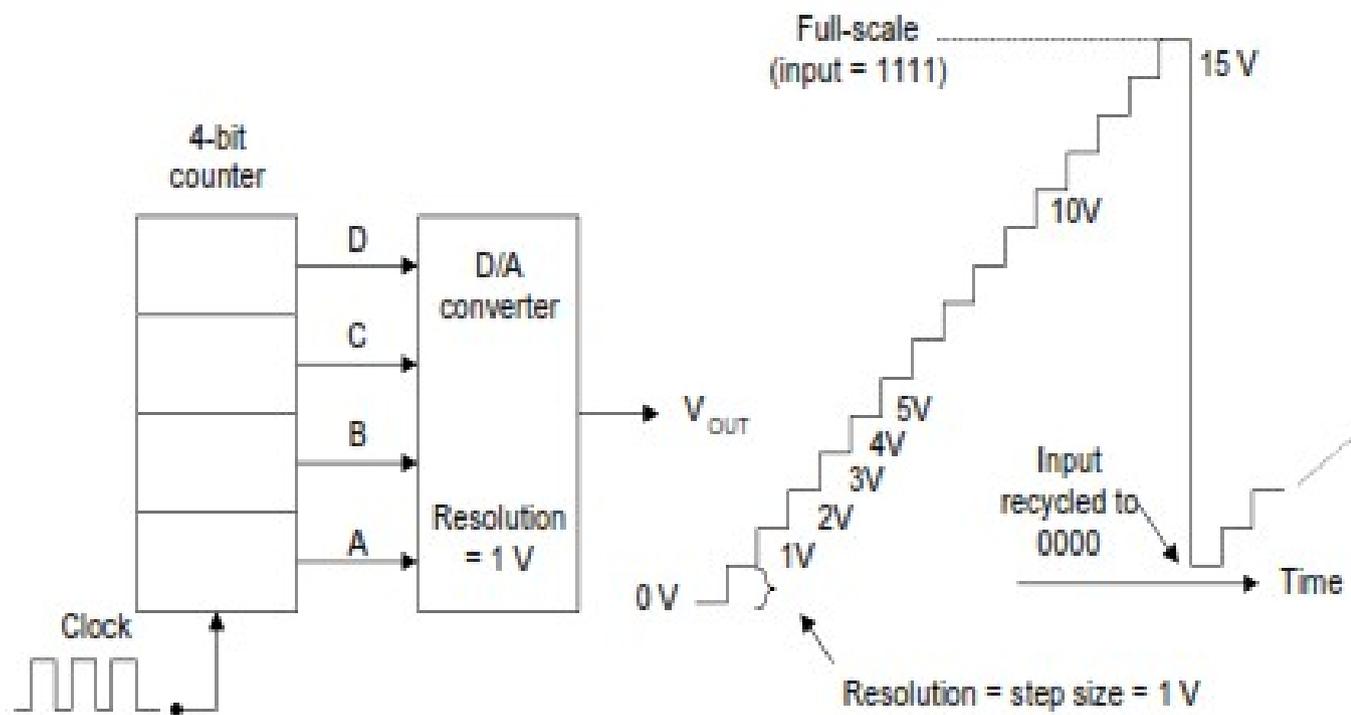


Fig. 7.3 : Output wave forms of a four bit DAC.

Other methods for finding analog o/p voltage or current

$$\text{analog output} = K \times \text{digital input}$$

where K is the proportionality factor and it is constant value for a given DAC. The analog output can of course be a voltage or current. When it is a voltage, K will be in voltage units, and when the output is current, K will be in current units. **K is the amount of voltage (or current) per step, i.e., $K = \text{step size}$**

Remember, the proportionality factor, K , will vary from one DAC to another.

The step size is 0.2 V, which is the proportionality factor K . The digital input is $10001 = 17_{10}$. Thus we have :

$$\begin{aligned} V_{\text{OUT}} &= (0.2 \text{ V}) \times 17 \\ &= 3.4\text{V} \end{aligned}$$

A 5-bit DAC has a current output. For a digital input of 10100, an output current of 10mA is produced. What will I_{OUT} be for a digital input of 11101?

Solution

The digital input 10100_2 is equal to decimal 20. Since $I_{OUT} = 10 \text{ mA}$ for this case, the proportionality factor as 0.5 mA. Thus, we can find for a digital input such as $11101_2 = 29_{10}$ as follows :

$$\begin{aligned} I_{OUT} &= (0.5\text{mA}) \times 29 \\ &= 14.5 \text{ mA} \end{aligned}$$

What is the largest value of output voltage from an 8-bit DAC that produces 1.0V for a digital input of 00110010?

Solution

$$00110010_2 = 50_{10}$$

$$1.0 \text{ V} = K \times 50$$

Therefore,

$$K = 20 \text{ mV}$$

The largest output will occur for an input of $11111111_2 = 255_{10}$.

$$V_{\text{OUT}}(\text{max}) = 20\text{mV} \times 255$$

$$= 5.10 \text{ V}$$

SPECIFICATIONS OF DAC (1)

- 1. Resolution :** The resolution of a DAC is a measure of the fineness of the increments between the output values.
 - For example a 4-bit DAC has a resolution of one part in $2^4 - 1$: $(1/15) * 100 = 6.67\%$.
- 2. Accuracy:** Accuracy is derived from a comparison of the actual output of a DAC with the expected output.
 - It is expressed as a percentage of a full-scale or maximum output voltage.
 - If a converter has a full-scale output of 10v and the accuracy is $\pm 0.1\%$, then the maximum error for any output voltage is $(10V)(0.001) = 10 \text{ mV}$

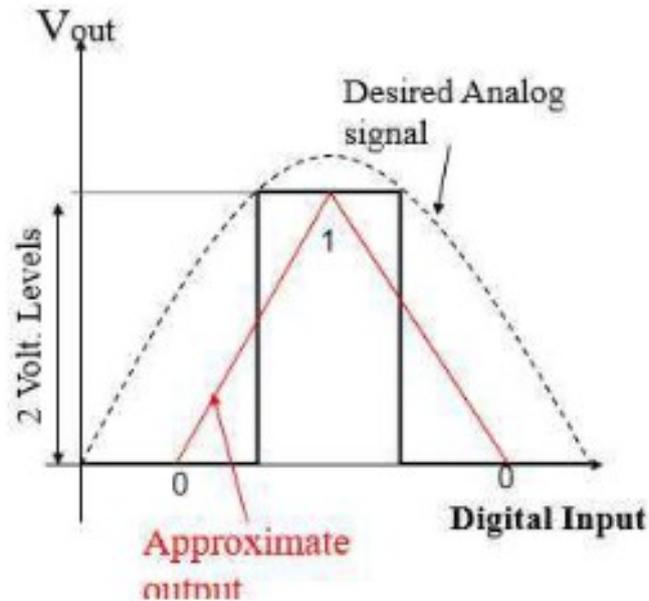
SPECIFICATIONS OF DAC (2)

- 3. Linearity:** A linear error is a deviation from the ideal straight-line output of a DAC.
 - A special case is an offset error, which is the amount of output voltage when the input bits are all 0's.
- 4. Monotonicity:** A DAC is monotonic if it doesn't take any reverse steps when it is sequenced over its entire range of input bits.
- 5. Settling Time:** Normally defined as the time it takes a DAC to settle within $\pm \frac{1}{2}$ LSB of its final value when a change occurs in the input code.

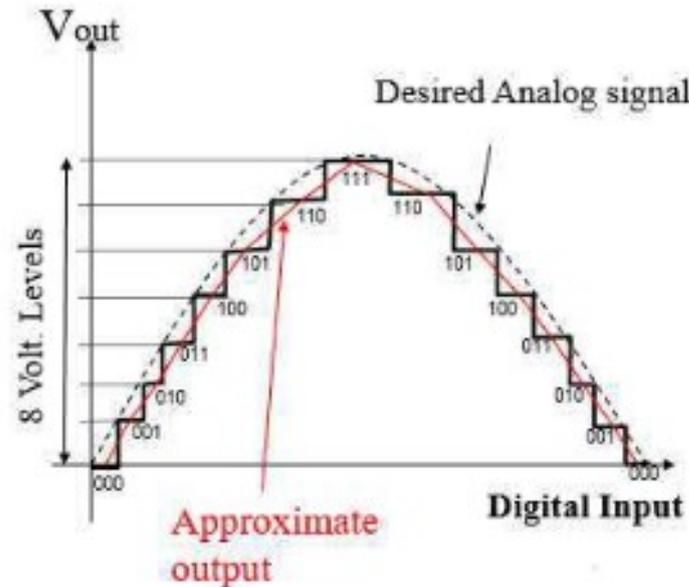
RESOLUTION

- **Resolution is the measure of how closely can we approximate the desired output signal (Higher Res. = finer detail = smaller Voltage divisions)**

Poor Resolution(1 bit)

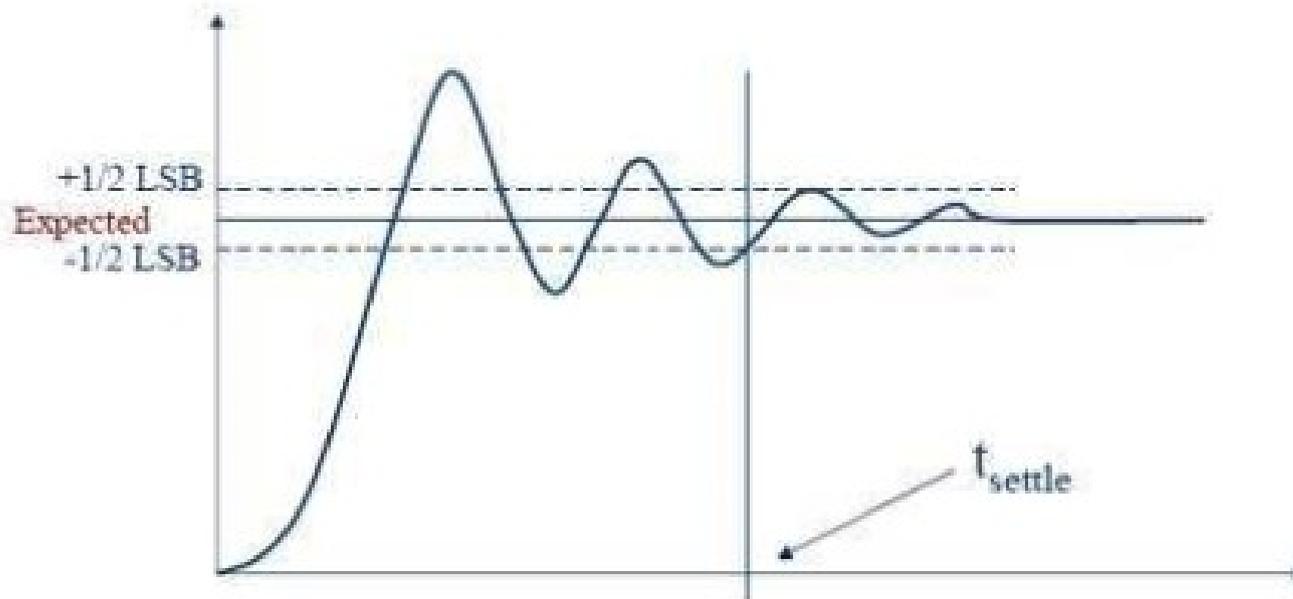


Better Resolution(3 bit)



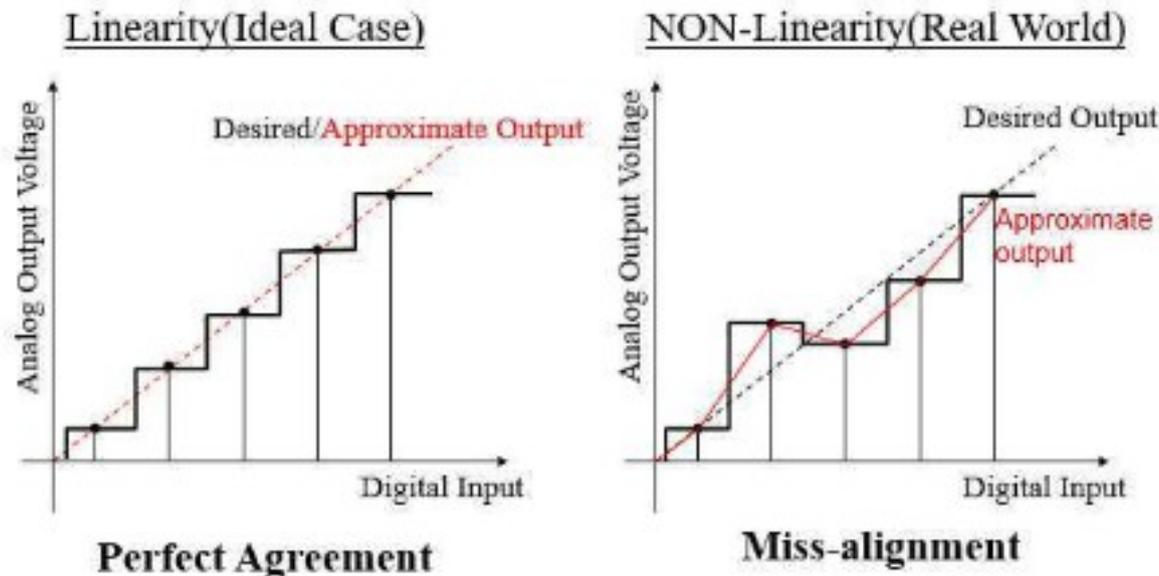
SETTLING TIME

- **Settling Time:** The time required for the input signal voltage to settle to the expected output voltage (within $\pm V_{\text{LSB}}$).
- Any change in the input state will not be reflected in the output state immediately.
- It is also called conversion speed.



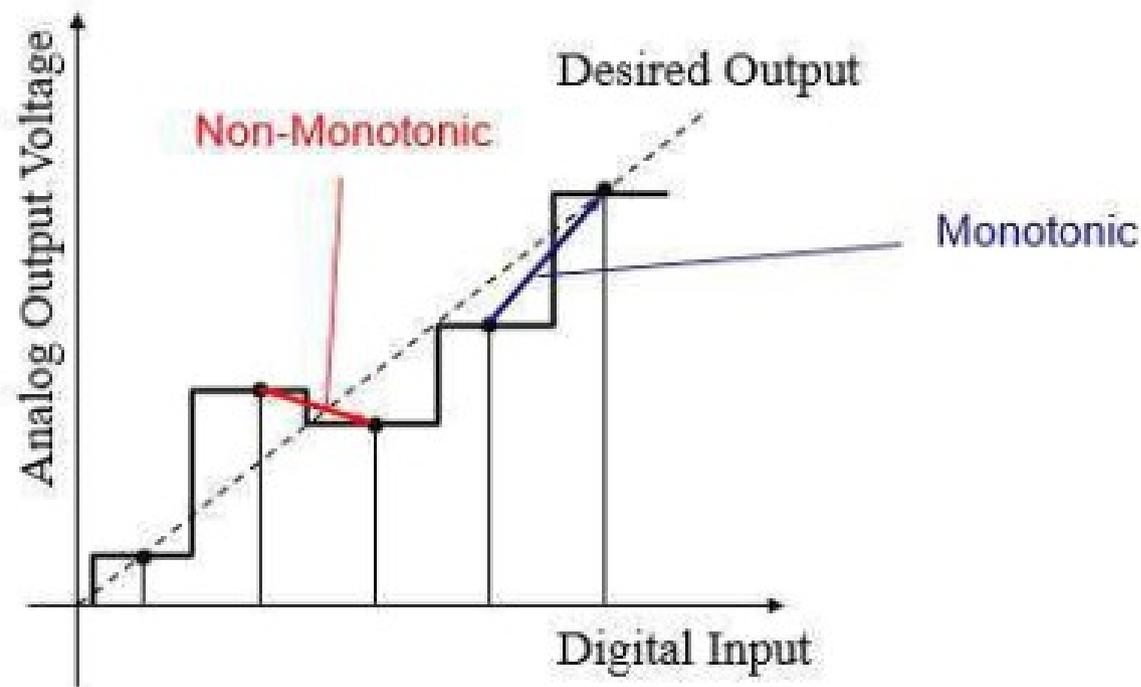
LINEARITY

- **Linearity**: is the difference between the desired analog output and the actual output over the full range of expected values.
- Ideally, a DAC should produce a linear relationship between a digital input and the analog output, this is not always the case.



MONOTONICITY

- A DAC is Monotonic if its output increases or remains the same for an increment in the Digital Code.
- Conversely, a DAC is Non-Monotonic, if the Output decreases for an increment in the Digital Code.



ACCURACY

- The Accuracy of a DAC is the difference between output practical analog output to the ideal expected output for a given digital input.
- For an example if a DAC of 10 V is said to have an accuracy of 0.01% there will be 10mv output deviation.
- Accuracy is measured in terms of the DAC offset error, gain error and Linearity issues.

